	INTRODUCTION		xiv
Chapter 1			
	FREE EXPLORATION		xvii 2
	Introducing materials	2	
	Storage	4	
	Establishing groundrules	5	
		NSION OF FREE EXPLORATION	
	The Jars	8	
	Weighing Common Objects	s 9	
	Mirrors	10	
	Food Coloring	11	
	Reproducing Designs	12	
	QUESTIONS FROM TEACI	HERS	14
Chapter 2	PATTERN ONE		18
•	INTRODUCTION		20
	Rhythmic Clapping	21	
	The Dot Chart	23	
	Unifix Patterns	26	
	People Row Patterns	29	
	APPLICATION AND EXTER	NSION OF PATTERN	3
	Unifix Snap and Clap		
	Patterns	33	
	The Dot Patterns	35	
	Geoboard-Unifix Patterns	36	
	Geoboard Sequences	37	
	Pattern Block Walls	38	
	Junk Pattern Cards	40	
	Border Patterns	41	
	Necklace Patterns	42	
	Learning to Write		
	Numerals	42	
	Large Numeral Cards	44	
	Cookie Dough Numerals	44	
	Numeral Sequence Cards	45	
	Geoboard Numerals	47	
	Dot to Dots	48	
	The Number Line	40	
	Templates	49	
	Writing Papers QUESTIONS FROM TEAC	50	52

Chapter 3	SORTING AND CLASSIF	VING	56
	INTRODUCTION		58
	Sorting on the Overhead		50
	Projector	59	
	People Sorting	61	
	Junk Box Sorting	64	
	APPLICATION AND EXTI		
	SORTING AND CLAS		70
	Read My Mind	70	
	Sorting and	10	
	Classifying Walks	72	
	Descriptions	72	
	Sorting by Senses	74	
		76	
	Name Hops	78	
	Geoboard Sorting Game	80	
	Geoboard Paths	81	
	Geoboard Arrow Game	82	
	Food Coloring	83	
	QUESTIONS FROM TEAC	CHERS	84
Chapter 4			
JIIapici 4	COUNTING		88
	INTRODUCTION		90
	Counting Forward	92	
	Count and Turn	93	
	The Counting Tape	94	
	The Pendulum Game	95	
	People Counting Game	96	
	The Circle Game	98	
	INVARIANCE OR CONSE	RVATION OF NUMBER	10
	The Piggy Bank Game	101	
	Spill the Beans	102	
	Changing Chairs	102	
	COUNTING ON		10;
	Cover Up	104	
	Bite Your Tongue	105	
	COUNTING BACKWARD		106
	Earlier States	107	100
	Snap and Clap	108	
	Stand Up, Sit Down	109	
	Take Over	110	
	Inside, Outside	111	
	QUESTIONS FROM TEAC		112
	delonono mom TEAC		114
Chapter 5	COMPADING		
			114
	INTRODUCTION		116
	Things in the Room	117	
	Comparing Names Height Records	118	
		119	

	Body Measurements 120	
	Teeter-Totter 122	
	APPLICATION AND EXTENSION OF COMPARI	NG 12
	Water Timer 123	
	Duration 124	
	Handfuls 125	
	Stack, Tell, Spin, and Win 126	
	Tic Tac Toe 128 The Hole in the Box 129	
	Squares 130	
	Measuring with Jars 131	
	Weighing and	
	Comparing 132	
	Intervals of Time 133	
	Measuring Strings 135	
	Mark the Scoops 136	
	<b>QUESTIONS FROM TEACHERS</b>	13
Chapter 6		
	GRAPHING	14
		14
	Real Graphs Comparing Two Groups 146	
	Real Graphs Comparing	
	Three Groups 147	
	Picture Graphs Comparing	
	Two Groups 148	
	Picture Graphs Comparing	
	Three Groups 149	
	Real Graphs Comparing	
	Four Groups 150	
	Picture Graphs Comparing	
	Four Groups 151	
	Symbolic Graphs Com-	
	paring Two Groups 152	
	Symbolic Graphs Com-	
	paring Three Groups 153	
	Symbolic Graphs Com-	
	paring Four Groups 154	0 11
	APPLICATION AND EXTENSION OF GRAPHIN Other Graphs 155	G 1
	QUESTIONS FROM TEACHERS	15
Chapter 7		
Chapter 7	NUMBER AT THE CONCEPT LEVEL	16
	INTRODUCTION	16
	The Number Stations:	
	Toothpicks 168	
	Tiles 169	
	Pattern Blocks 170	
	A	

171         bes       172         Cubes       173         174       174         es       175         ds       176         the       5         Stations       177         NAND EXTENSION OF         AT THE CONCEPT LEVE         ames:         Game       180         owl       181         ough         /all       183         othe       186         ame       188         ount       190         191       192         cards       193	EL 179
Cubes         173           174         175           es         175           ds         176           the         177           Stations         177           N AND EXTENSION OF         AT THE CONCEPT LEVE           ames:         Game         180           owl         181           ough         183           g the         186           ame         188           ount         190           191         192	EL 179
174         es       175         is       176         the       5         Stations       177         NAND EXTENSION OF       AT THE CONCEPT LEVE         ames:       6         Game       180         owl       181         ough       183         og the       186         ame       188         ount       190         191       192	EL 179
es 175 ds 176 the Stations 177 NAND EXTENSION OF AT THE CONCEPT LEVE ames: Game 180 owl 181 ough /all 183 g the mes 186 ame 188 ount 190 n 191 192	EL 179
ds 176 the Stations 177 NAND EXTENSION OF AT THE CONCEPT LEVE ames: Game 180 owl 181 ough /all 183 g the mes 186 ame 188 ount 190 n 191 192	<u>EL 179</u>
the Stations 177 NAND EXTENSION OF AT THE CONCEPT LEVE ames: Game 180 owl 181 ough /all 183 g the mes 186 ame 188 ount 190 1 191 192	EL 179
Stations 177 NAND EXTENSION OF AT THE CONCEPT LEVE ames: Game 180 owl 181 ough Vall 183 g the mes 186 ame 188 ount 190 1 191 192	EL 179
Stations 177 NAND EXTENSION OF AT THE CONCEPT LEVE ames: Game 180 owl 181 ough Vall 183 g the mes 186 ame 188 ount 190 1 191 192	EL 179
AT THE CONCEPT LEVE ames: Game 180 owl 181 ough /all 183 g the mes 186 ame 188 ount 190 n 191 192	<u>EL 179</u>
ames: Game 180 owl 181 ough /all 183 g the mes 186 ame 188 ount 190 n 191 192	<u>=L 179</u>
Game       180         owl       181         ough       183         /all       183         g the       186         mes       186         ame       188         ount       190         191       192	
owl 181 bugh /all 183 g the mes 186 ame 188 bunt 190 n 191 192	
bugh Vall 183 g the mes 186 ame 188 bunt 190 n 191 192	
/all 183 g the mes 186 ame 188 punt 190 n 191 192	
g the mes 186 ame 188 punt 190 n 191 192	
mes 186 ame 188 ount 190 n 191 192	
ame 188 ount 190 n 191 192	
ount 190 n 191 192	
n 191 192	
192	
	*
ards 193	
195	
196	
e-O 197	
Jp'' 200	
202	
FROM TEACHERS	210
THE CONNECTING LEVE	
	216
	UMBER AT 221
	22
-	
228	
olume 232	
	THE CONNECTING LEVE ON ymbols 217 s 219 N AND EXTENSION OF N INECTING LEVEL ymbols to ames 221 225 dome 226 ace 227 Jp

ix

Chapter 9	NUMBER AT THE SYMBOLIC LEVEL	23
		23
	The Old Games 237	
	APPLICATION AND EXTENSION OF NUMBER AT THE SYMBOLIC LEVEL	24
	Numbered Squares 243	
	Growing Plants 244	
	Dice Toss 244	
	A Rock Bath 245	
	The Grab Bag 246	
	Addition with	
	Unifix Cubes 246	
	Time Trials 247	
	Number Sequences 248	
	The Magic Box 248	
	QUESTIONS FROM TEACHERS ON NUMBER AT	
	THE CONNECTING AND SYMBOLIC LEVELS	25
Chapter 10	Concentration - Connection - Connection	
	PATTERN TWO	25
	INTRODUCTION	25
	Fruit and	
	Vegetable Patterns 254	
	Leaf Patterns 256	
	Clothing Patterns 257	
	Matrix Patterns 258	
	Routes 259	
	Geoboard Number	
	Patterns 260	
	Tile Patterns 261	
	Surrounding Patterns 265	
	Row, Column, and	
	Diagonal Patterns	
	With Unifix Cubes 267	
	Names 270	
	QUESTIONS FROM TEACHERS	27
hontor 11		
hapter 11	PLACE VALUE	27
	INTRODUCTION	27
	The Place Value	
	Counting Game	
	Concept Development	
	Stage 276	
	Connecting Symbols	
	to the Concept 294	
	Using Symbols	
	to Record	
	The Concept 299	
	APPLICATION AND EXTENSION OF PLACE VALUE	30

			1
	Measuring	307	
	Estimating and Checking	308	
	Counting Jars of Objects	310	
	Peas in the Pod	311	
	Determining Prices	312	
	Base Ten Unifix Patterns	314	
	Perimeters	315	
	Geoboard Designs The Store	316	
	The Movie Theatre	317 318	
	Estimating and Graphing	319	
	Unifix Stacks	320	
	Recording Number	020	
	Patterns from Row,		
	Column, and		
	Diagonal Patterns		
	with Unifix Cubes	321	
	Recording Number		
	Patterns from		
	Surrounding		
	Patterns	323	
	QUESTIONS FROM TEAC	CHERS	324
Chapter 10			
Chapter 12	PATTERN BOOK EXPERI	MENTS	326
			328
	Eyes	329	<u>328</u>
	Eyes Stars	329 330	<u>328</u>
	Eyes Stars Popsicles	329 330 331	<u>328</u>
	Eyes Stars Popsicles Hands	329 330 331 331	<u>328</u>
	Eyes Stars Popsicles Hands Money	329 330 331 331 332	<u>328</u>
	Eyes Stars Popsicles Hands	329 330 331 331	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares	329 330 331 331 332 333	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers	329 330 331 331 332 333 335 335 335 336	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles	329 330 331 331 332 333 335 335 336 337	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands	329 330 331 331 332 333 335 335 336 337 338	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction	329 330 331 331 332 333 335 335 335 336 337 338 339	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge	329 330 331 331 332 333 335 335 335 336 337 338 339 340	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids	329 330 331 331 332 333 335 335 335 336 337 338 339	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House	329 330 331 331 332 333 335 335 335 336 337 338 339 340 340	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager	329 330 331 331 332 333 335 335 336 337 338 339 340 342 343	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate	329 330 331 331 332 333 335 335 336 337 338 339 340 342 343 345	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away	329 330 331 331 332 333 335 335 336 337 338 339 340 342 343	<u>328</u>
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away Milk Carton	329 330 331 331 332 333 335 335 335 336 337 338 339 340 342 343 345 346	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away Milk Carton Clothespin Game	329 330 331 331 332 333 335 335 336 337 338 339 340 342 343 345 346 347	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away Milk Carton	329 330 331 331 332 333 335 335 335 336 337 338 339 340 342 343 345 346	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away Milk Carton Clothespin Game Count the Squares	329 330 331 331 332 333 335 335 335 336 337 338 339 340 342 343 345 346 347 348	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away Milk Carton Clothespin Game Count the Squares Pattern Block Puzzles	329 330 331 331 332 333 335 335 336 337 338 339 340 342 343 345 346 347 348 349	328
	Eyes Stars Popsicles Hands Money Toothpick Squares Jumping Rope Glasses Three Leaf Clovers Triangles Joining Hands A Chain Reaction London Bridge Pyramids Apartment House Manager Karate Two-handed Take Away Milk Carton Clothespin Game Count the Squares Pattern Block Puzzles Geoboard Nails	329 330 331 331 332 333 335 335 336 337 338 339 340 342 343 345 346 347 348 349 351	328